

2014학년 1학기

수학전공 Colloquium

◆ 제 목 : Leray's inequality in multi-connected domains.

◆ 연 사 : Hideo Kozono (Waseda)

◆ 초 록 : Consider the stationary Navier–Stokes equations in a bounded domain $\Omega \subset \mathbb{R}^n$ whose boundary $\partial\Omega$ consists of $L+1$ disjoint closed C^∞ -surfaces $\Gamma_0, \Gamma_1, \dots, \Gamma_L$ with $\Gamma_1, \dots, \Gamma_L$ inside of Γ_0 . The Leray inequality of the given boundary data β on $\partial\Omega$ plays an important role for the existence of solutions. It is known that if the flux $\gamma_i \equiv \int_{\Gamma_i} \beta \cdot \nu dS = 0$ on Γ_i (ν : the unit outer normal to Γ_i) is zero for each $i = 0, 1, \dots, L$, then the Leray inequality holds. We prove that if there exists a sphere S in Ω separating $\partial\Omega$ in such a way that $\Gamma_1, \dots, \Gamma_k$, $1 \leq k \leq L$ are contained in S and that $\Gamma_{k+1}, \dots, \Gamma_L$ are in the outside of S , then the Leray inequality necessarily implies that $\gamma_1 + \dots + \gamma_k = 0$. In particular, suppose that for each $i = 1, \dots, L$ there exists a sphere S_i in Ω such that S_i contains only one Γ_i . Then the Leray inequality holds if and only if $\gamma_0 = \gamma_1 = \dots = \gamma_L = 0$.

◆ 일 시 : 4월 8일(화) 오후 5시

◆ 장 소 : 5동 102